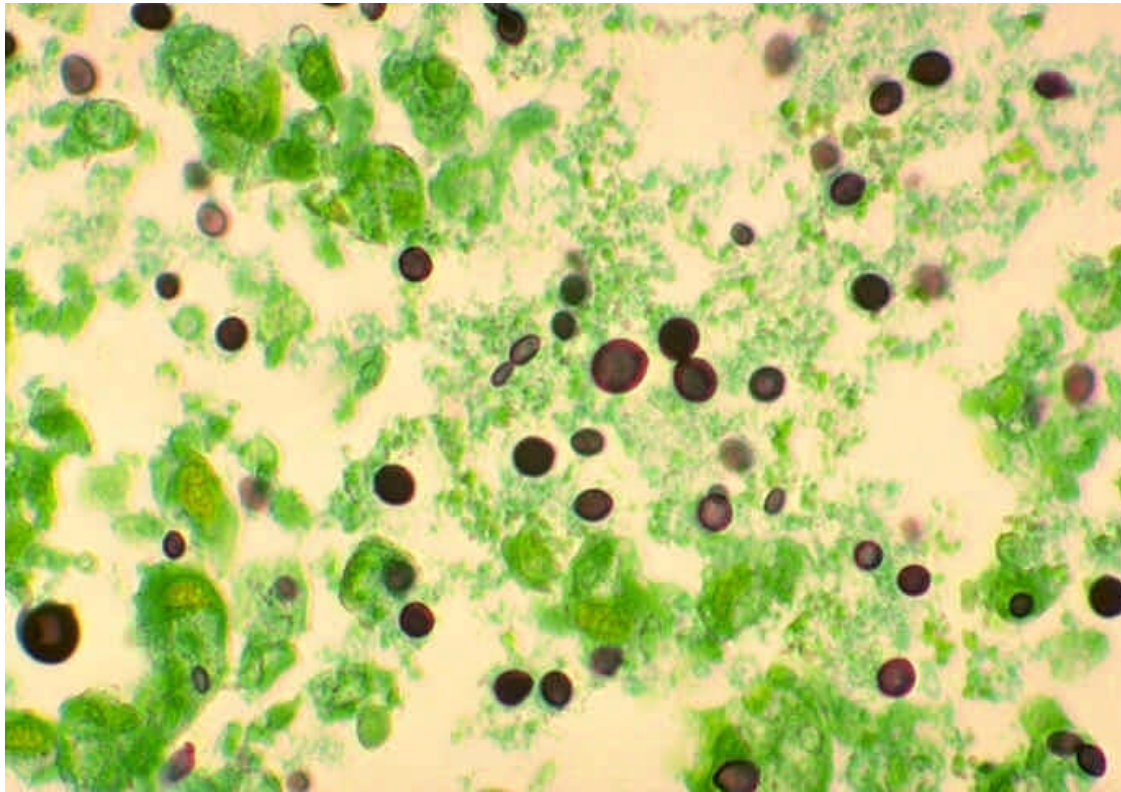


# Approaches for classification and counting by image analyses



**A. Conci**  
**[aconci@ic.uff.br](mailto:aconci@ic.uff.br)**

**UFF**  
**Universidade Federal**  
**Fluminense**  
**Brazil**

# Applications:

- ceramic micrography
- petrology and petrography
- mineralogy
- metallurgy
- quality controls
- biological cells
- medical exams
- geology
- civil engineering
- astronomy
- microscopic analysis



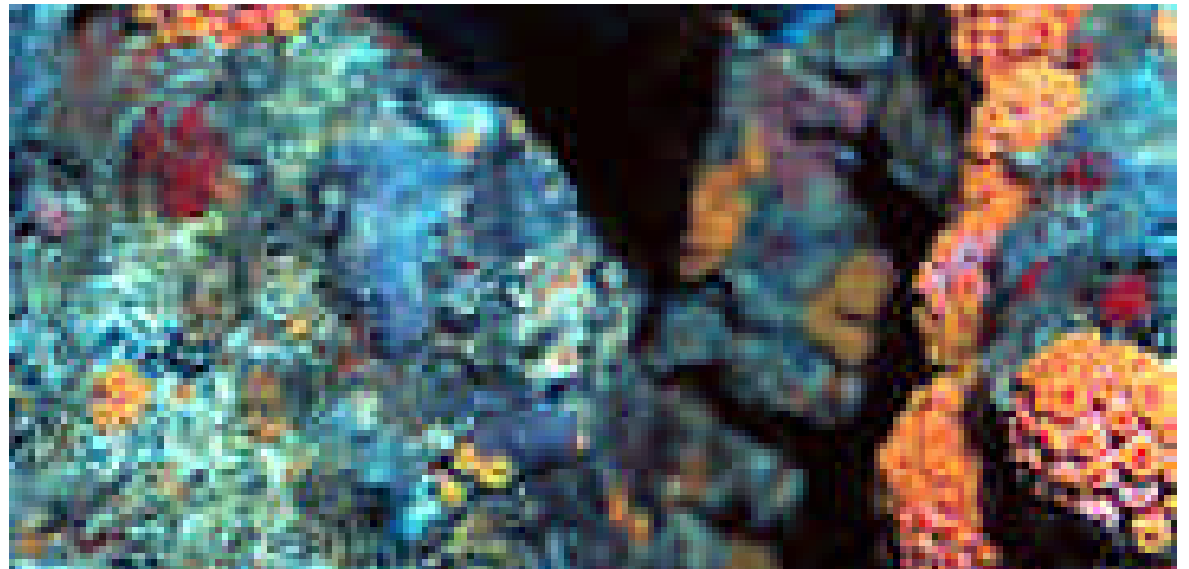
**Particles size distribution and identification =  
granulometry**

**Granulometry by using:**

**mathematical morphology;**

**best fitting shapes;**

**Hough Transform;**



# Counting Cells by Mathematical Morphology

- **Main idea:** image simplification by removing not relevant details **preserving** essential characteristics of **form**
- Basic operations : **dilation, erosion, opening and closing**



# Dilation on gray value image

- are defined by:

$$f \oplus k = (f \oplus k)(x) = \max \{ z \in K, x-z \in F \mid f(x-z) + k(z) \}$$

where  $F, K$  be the domains of functions:  $f(x, y)$  and  $k(x, y)$ ,  
 $x, y \in \mathbb{Z}$

- it gives an "expansion" or "grow" on the image

|   | 0 | 1   | 2 | 3  | 4 |
|---|---|-----|---|----|---|
| 0 |   |     |   |    |   |
| 1 |   |     | 3 | 40 |   |
| 2 |   |     |   |    |   |
| 3 |   |     |   |    |   |
| 4 |   | 30  |   | 55 |   |
| 5 |   |     |   |    |   |
| 6 |   |     |   |    |   |
| 7 |   |     |   |    |   |
| 8 |   | 120 |   |    |   |
| 9 |   |     |   |    |   |

(a)

|    |    |    |
|----|----|----|
|    | 10 |    |
| 10 | 10 | 10 |
|    | 10 |    |

(b)

|   | 0   | 1   | 2   | 3  | 4  |
|---|-----|-----|-----|----|----|
| 0 |     |     | 13  | 50 |    |
| 1 |     | 13  | 50  | 50 | 50 |
| 2 |     |     | 13  | 50 |    |
| 3 |     | 40  |     | 65 |    |
| 4 | 40  | 40  | 65  | 65 | 65 |
| 5 |     | 40  |     | 65 |    |
| 6 |     |     |     |    |    |
| 7 |     | 130 |     |    |    |
| 8 | 130 | 130 | 130 |    |    |
| 9 |     | 130 |     |    |    |

(c)

- $f$  is normally the image, while  $k$  is named **structuring element**

# Dilation on color image

- each **RGB**, **HSV** or **YIQ** channel must be considered



**$3 \times 3\{1\}$  for each channel: *red, green e blue***

**original**



**result**



## Erosion on gray value image:

- Let  $F, K$  be the domains of functions:  $f(x, y)$  and  $k(x, y)$

where  $x, y \in \mathbb{Z}$ , then Erosion can be defined as:

$$f \ominus k = \min \{ z \in K, x+z \in F \mid f(x+z) - k(z) \}$$

|   | 0  | 1   | 2  | 3   | 4 |
|---|----|-----|----|-----|---|
| 0 |    |     |    | 66  |   |
| 1 |    |     | 3  | 40  | 7 |
| 2 |    |     |    | 150 |   |
| 3 |    |     |    |     |   |
| 4 |    | 30  |    | 55  |   |
| 5 |    |     |    |     |   |
| 6 |    |     |    |     |   |
| 7 |    | 70  |    |     |   |
| 8 | 95 | 120 | 12 |     |   |
| 9 |    | 40  |    |     |   |

(a)

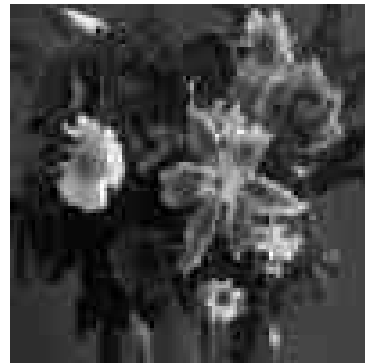
|    |    |    |
|----|----|----|
|    | 10 |    |
| 10 | 10 | 10 |
|    | 10 |    |

(b)

|   | 0 | 1 | 2 | 3 | 4 |
|---|---|---|---|---|---|
| 0 |   |   |   |   |   |
| 1 |   |   |   |   |   |
| 2 |   |   |   |   |   |
| 3 |   |   |   |   |   |
| 4 |   |   |   |   |   |
| 5 |   |   |   |   |   |
| 6 |   |   |   |   |   |
| 7 |   |   |   |   |   |
| 8 |   | 2 |   |   |   |
| 9 |   |   |   |   |   |

(c)

## Erosion results to color images:



**$3 \times 3\{1\}$  for each channel: *red, green e blue***

**original**



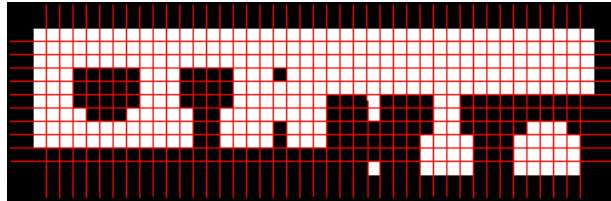
**result**





# Closing and opening

- These operations are a combination of dilation and erosion:  
original image:



Erosion of the original image  
by a 3 x 3 structural element



Dilation by a 3 x 3 structural  
element.



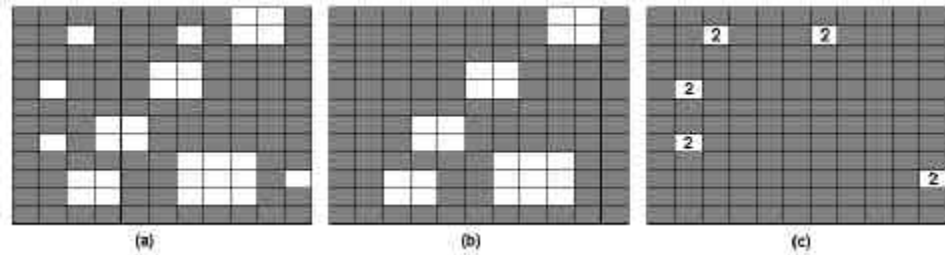
Followed by a dilation of the  
previous eroded image = **opening**



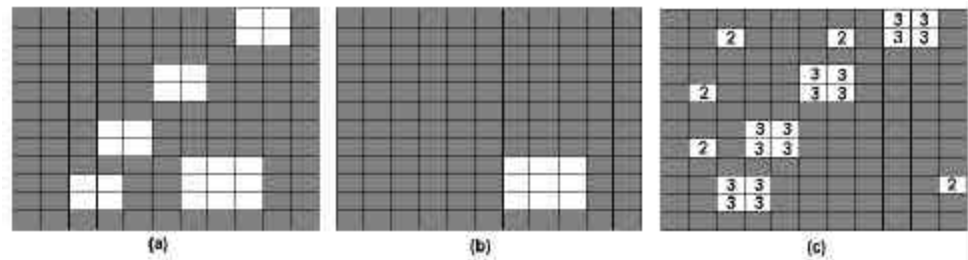
Followed by a erosion of the  
previous dilated image = **closing**

# Morphological Granulometrie:

set of Opening using  $I \ B$   
( series of virtual **sieve** with  
meshed defined by the  
**structuring element** size )



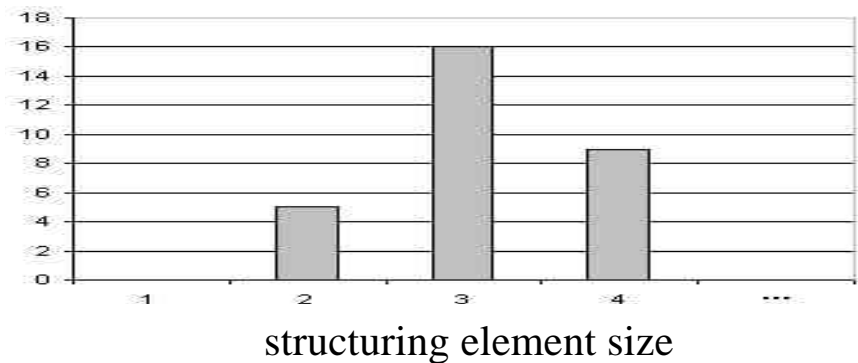
1st step: (a) original image, (b) open by a square **2x2**, (c) result



2nd step: (a) Image of first step (b) open by a square **3x3**, (c) result

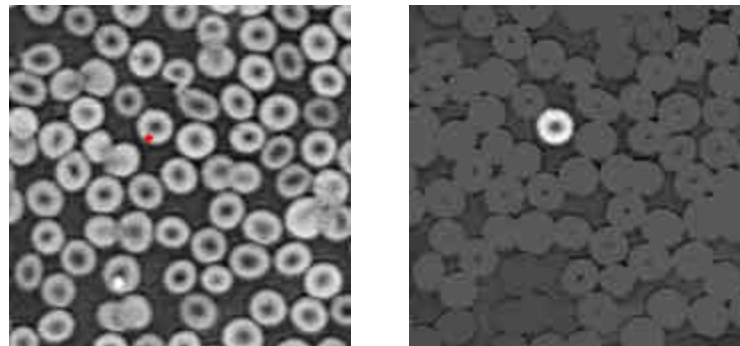
etc. to size distribution:

Number  
of  
pixels  
erased  
in  
the  
image

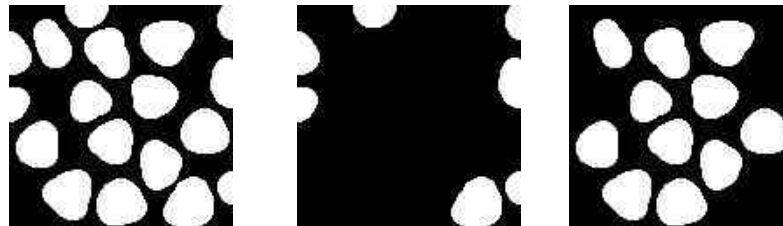


# Morphological Reconstruction

- inserts the **concept of connectivity** in images;
- **with** Reconstruction :
  - only **complete cells eliminated** by opening using  $I \ominus B$
  - elements **inside** cells can be identify

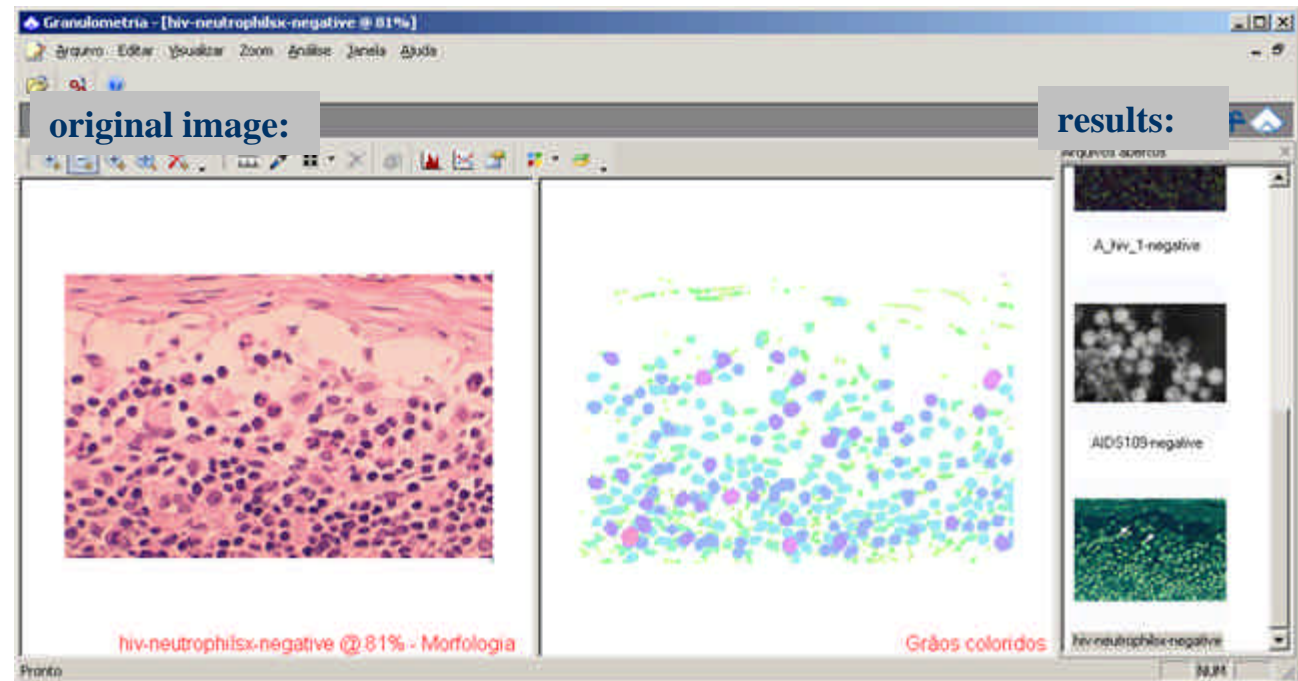


- only **complete cells** in the frame are counted



Example:

extract  
blood and  
HIV cells and  
from microscopic



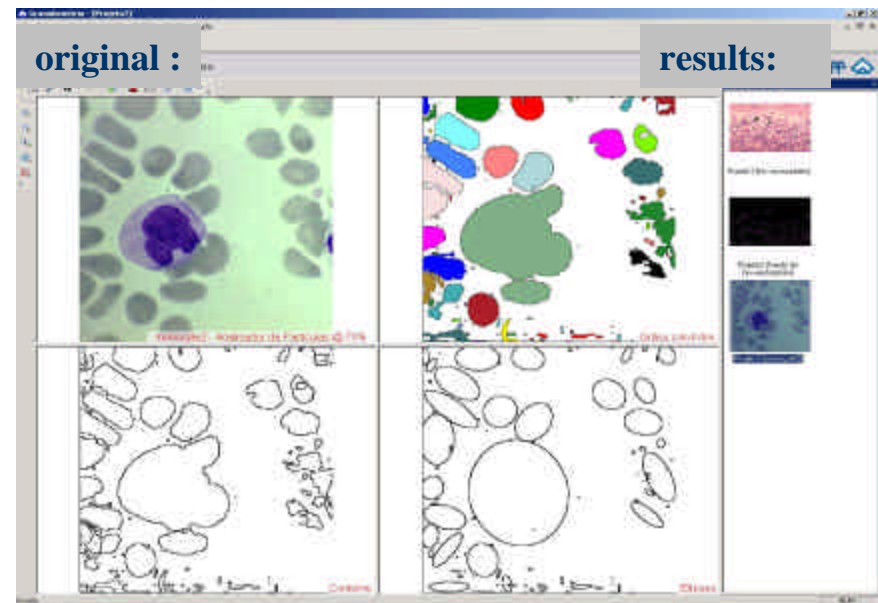
(different color => different number of nuclei)

# Granulometry by using best fitting shapes

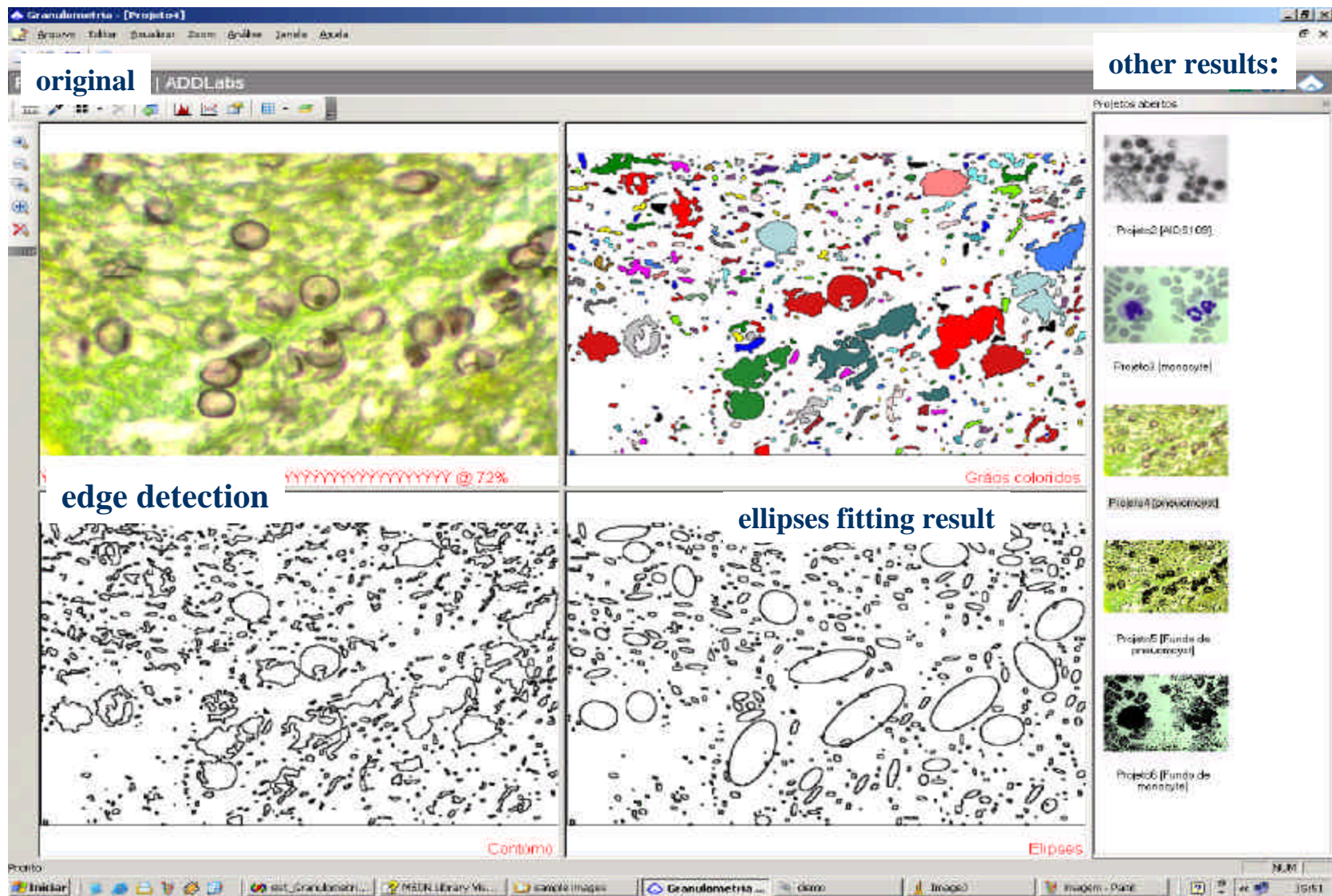
Hybrid image

processing techniques:

- background extraction
- HSV color space
- windowed threshold
- adaptive edge segmentation
- ellipses fitting of the cells



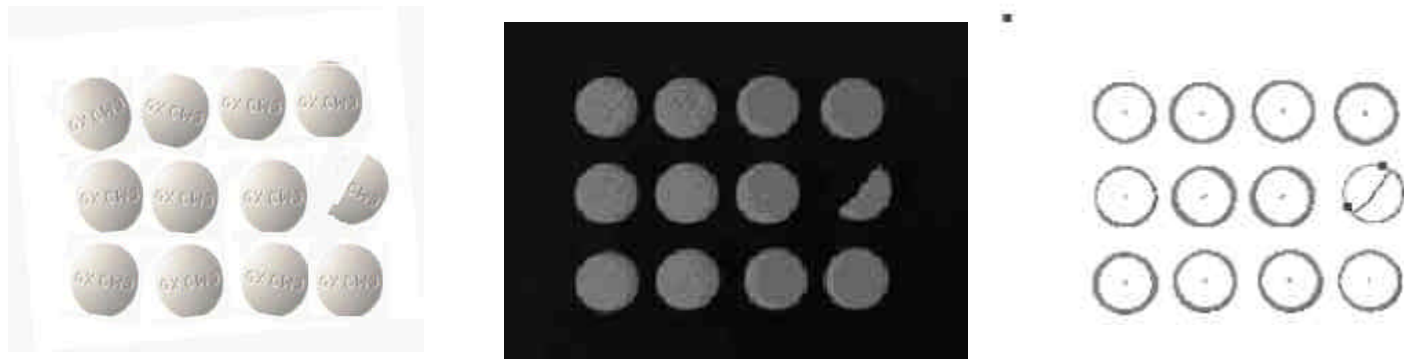
Example on cell identification and counting:





## Granulometry by Hough Transform

Main idea use of Hough transform methodology for detection of circle, arcs and ellipses of predefined dimension and perfect shape



Examples on detect fails in the industrial production of pills

# Conclusions

- **Mathematical Morphology**
  - can be used for
    - 3D and 2D elements
    - color ,
    - gray scale
    - binary images
    - partial elements
    - can recognize
      - inside properties
      - all shapes
- **Limits of others approaches:**
  - image processing techniques:
    - touching shapes
  - **Hough Transform**
    - only shapes with known equations

